

**SEMM 1921  
INTRODUCTION TO MECHANICAL  
ENGINEERING**

**PROBLEM SOLVING  
SKILLS**

# 1.3 Problem Solving Skills

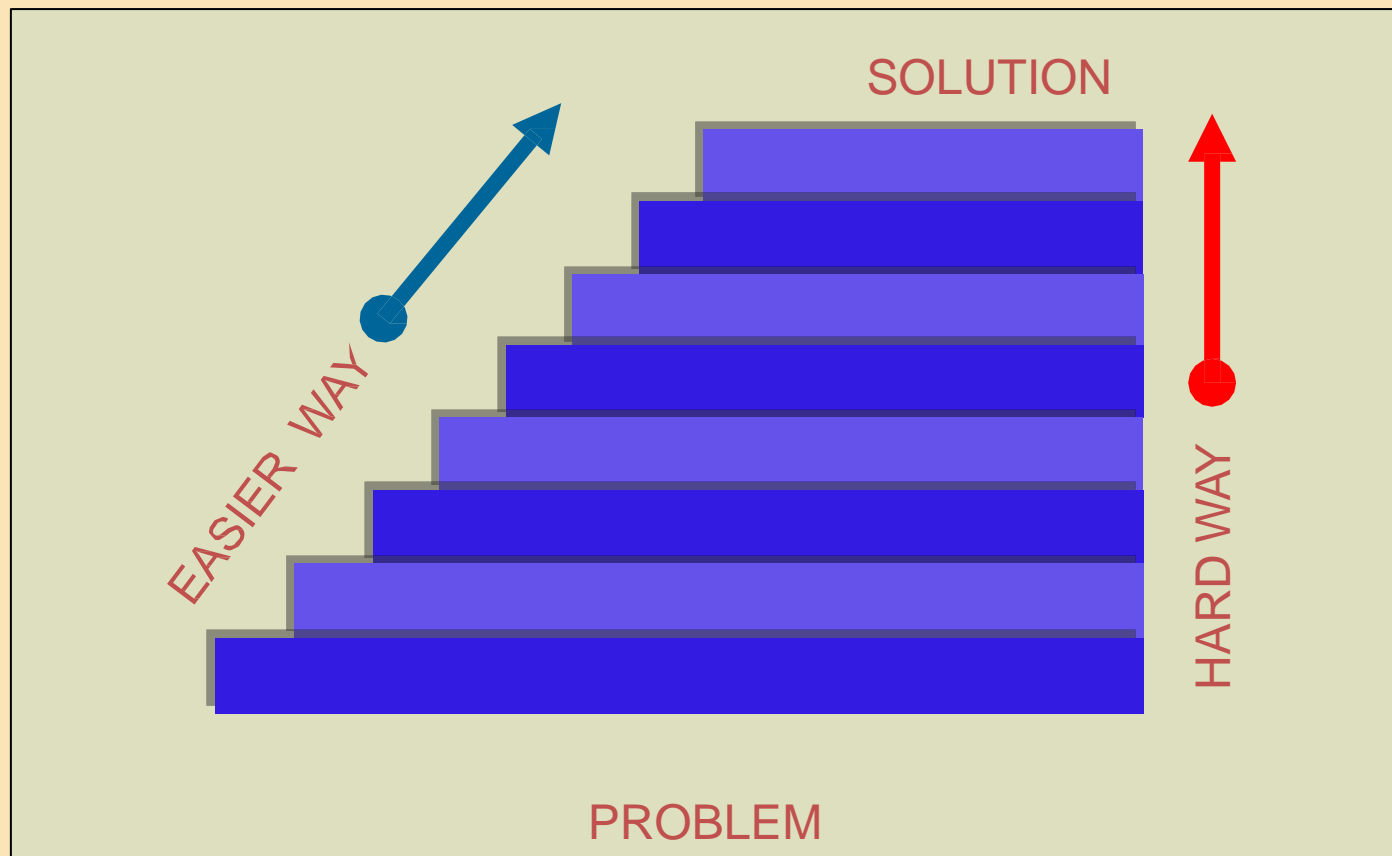
- 1.3.1 Why Problem Solving is Important?
  - Engineers by definition are problem solvers
  - Whether they are involved in analytical, experimental, computational or design work, engineers solve problems
  - In professional practice, engineers commonly solve problems that are highly complex and open-ended
  - Good engineering requires high-level thinking

# 1.3 Problem Solving Skills

- 1.3.1 Why Problem Solving is Important?
  - Professor Woods and his colleagues at McMaster University define problem solving as:
    - "Problem solving is the process of obtaining a **satisfactory** solution to a **novel problem**, or at least a problem which the problem solver has **not seen before**."
  - Real world problems tend to be quite different than most exercises found in engineering textbooks
  - Many studies have found that engineering graduates, even though they solve more than 2,500 exercises in their undergraduate work, lack the essential problem solving skills needed to tackle real world problems

# 1.3 Problem Solving Skills

- 1.3.2 Problem Approach



# 1.3 Problem Solving Skills

- 1.3.2 Problem Solving Approach
  - Wood's Method [2,3]

STEPS	DESCRIPTION
0. Engage/Motivation	I can do it! I want to do it!
1. Define the Problem	<ul style="list-style-type: none"><li>✓ Define what the problem states</li><li>✓ Sketch the problem (if appropriate)</li><li>✓ Determine the given information</li><li>✓ Determine constraints</li><li>✓ Define criterion for judging final product</li></ul>
2. Explore the problem	<ul style="list-style-type: none"><li>✓ Determine the real objective of the problem</li><li>✓ Examine issues involved</li><li>✓ Make reasonable assumptions</li><li>✓ Guess/estimate the answer</li></ul>

# 1.3 Problem Solving Skills

- 1.3.2 Problem Solving Approach
  - Wood's Method

STEPS	DESCRIPTION
3. Plan the solution	<ul style="list-style-type: none"><li>✓ Develop a plan to solve the problem</li><li>✓ Map out sub-problems</li><li>✓ Select appropriate theory, principles, approach</li><li>✓ Determine info that needs to be found</li></ul>
4. Implement the plan	<ul style="list-style-type: none"><li>✓ Take actions</li><li>✓ Do calculations and analysis</li></ul>
5. Check the solution	<ul style="list-style-type: none"><li>✓ Units and accuracy</li></ul>
6. Evaluate/Reflect	<ul style="list-style-type: none"><li>✓ Is it reasonable? Does it make sense?</li><li>✓ Were the assumptions appropriate?</li><li>✓ How does it compare to initial guess/estimate?</li><li>✓ If appropriate, ask the question: is it socially / ethically acceptable?</li></ul>

# 1.3 Problem Solving Skills

- 1.3.2 Problem Solving Approach
  - Wales's Method – Professional Decision Making Process [4,5]

STEPS	DESCRIPTION
1. Affirmation	✓ Make statement(s) that promote effective psychological management
2. Define the situation	✓ Ask questions and gather appropriate information with an intent of clarifying, interpreting, and understanding the situation
3. State the goal	✓ Determine the appropriate or best goal or combination of goals. ✓ The goal should be concrete ✓ The goal should be presented with enough specificity so different people would agree when the goal is reached

# 1.3 Problem Solving Skills

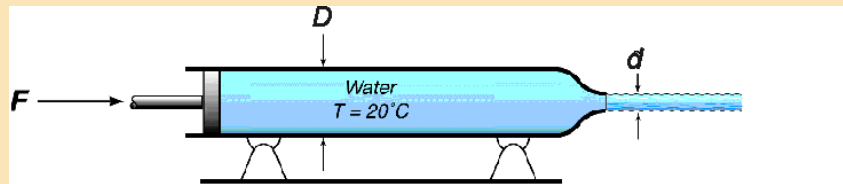
- 1.3.2 Problem Solving Approach
  - Wales's Method – Professional Decision Making Process

STEPS	DESCRIPTION
4. Generate Ideas	<ul style="list-style-type: none"><li>✓ Generate many possible ways to reach the goal</li><li>✓ Analyze these ideas, and then select the best idea or combination of ideas</li></ul>
5. Prepare a plan	<ul style="list-style-type: none"><li>✓ Carefully plan the steps needed to make the best idea a reality</li></ul>
6. Take action	<ul style="list-style-type: none"><li>✓ Implement the plan</li></ul>
7. Review & Reflect	<ul style="list-style-type: none"><li>✓ Check the solution to assess quality.</li><li>✓ Analyze the problem solving approach in order to identify what worked and what did not work</li><li>✓ Seek ways to refine or improve one's problem solving approach</li><li>✓ Clarify what was learned during the complete experience.</li></ul>



# 1.3 Problem Solving Skills

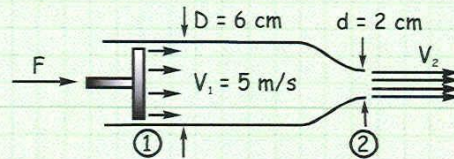
- 1.3.2 Problem Solving Approach
  - Professional Decision Making Process : An Example [4]
    - **5.52 Water is forced out of this nozzle by a piston moving at a speed of 5 m/s. Determine the force  $F$  required to move the piston and the speed of efflux of water from the nozzle. Neglect friction on the piston and assume irrotational flow. The exit pressure is atmospheric;  $D = 6$  cm and  $d = 2$  cm.**



Problem 5.52; from Crowe et al. (2001)

**AFFIRM**

I will practice skills that lead to excellence in professional practice!

**DEFINE THE SITUATION**

 Piston forces H<sub>2</sub>O out of nozzle

- \* Bernoulli eqn. applies
- \*  $p_2 = 0$  kPa-gage
- \*  $T = 20^\circ\text{C}$
- \* Assume steady flow
- \* Neglect friction on piston

**GOAL**
 $F$  (N)  $\Leftarrow$  Force to move piston

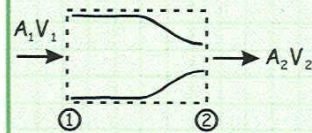
 $V_2$  (m/s)  $\Leftarrow$  Speed of jet

**GENERATE IDEAS**

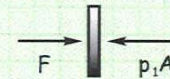
1. Conservation of Mass

2. Bernoulli Eqn.

3. Equilibrium



$$\frac{p_1}{\rho} + \frac{V_1^2}{2} = \frac{p_2}{\rho}$$


**PLAN**

G	E	N	I
$F$	$F = p_1 A_1$	$p_1$	$A_1 = \pi \cdot 0.03^2 \text{ m}$
$p_1$	$\frac{p_1}{\rho} + \frac{V_1^2}{2} = \frac{p_2}{\rho} + \frac{V_2^2}{2}$	$V_2$	$\rho = 1000 \text{ kg/m}^3, V_1 = 5 \text{ m/s}, p_2 = 0$
$V_2$	$V_2 = V_1 \left(\frac{D}{d}\right)^2$	none	$\frac{D}{d} = 3$

**ACTION**

$$1. V_2 = \left(\frac{5\text{m}}{\text{s}}\right)(3) = \underline{45 \text{ m/s}}$$

$$2. p_1 = \rho \frac{(V_1^2 - V_2^2)}{2} = \left(\frac{1000 \text{ kg}}{\text{m}^3}\right) \left(\frac{45^2 - 5^2 \text{ m}^2}{\text{s}^2}\right) \left(\frac{\text{Pa} \cdot \text{m}^2}{\text{kg}}\right) = 998 \text{ kPa}$$

$$3. F = p_1 A_1 = \left(\frac{998 \text{ kN}}{\text{m}^2}\right) \left(\frac{\pi \cdot 0.06^2 \text{ m}^2}{4}\right) = \underline{2.82 \text{ kN}}$$

**REVIEW**

1.  $p_1$  is about 10 atm; make sure pipe material is strong  
Force on piston is about 600 lbf
2. GENI worked well; next time double check problem statement
3. Jet speed about 90 mph--is this a safety issue ??
4. REMEMBER--Contracting flow ==> good use of Bernoulli eqn.

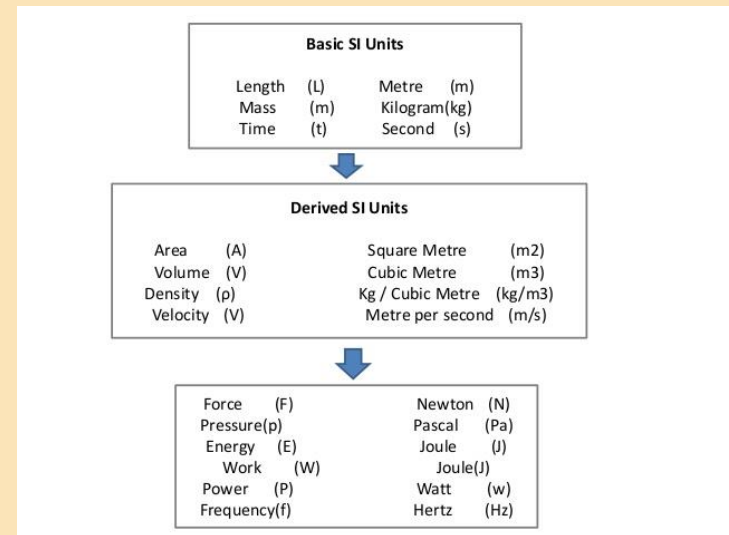
# UNIT SYSTEMS AND CONVERSIONS

Engineers specify physical quantities in two different—but conventional—systems of units:

- 1) United States Customary System (USCS)
- 2) International System of Units (Système International d'Unités or SI).

Practicing mechanical engineers must be conversant with both systems. They need to convert quantities from one system to the other, and they must be able to perform calculations equally well in either system.

Typical Mechanical Properties of Carbon–Carbon Matrix Composites				
Property	Units	C-C	Steel	Aluminum
<i>System of units: USCS</i>				
Specific gravity	—	1.68	7.8	2.6
Young's modulus	Msi	1.95	30	10
Ultimate tensile strength	ksi	5.180	94	40
Coefficient of thermal expansion	μin./in./°F	1.11	6.5	12.8
<i>System of units: SI</i>				
Specific gravity	—	1.68	7.8	2.6
Young's modulus	GPa	13.5	206.8	68.95
Ultimate strength	MPa	35.7	648.1	234.4
Coefficient of thermal expansion	μm/m/°C	2.0	11.7	23



To Convert from U.S. Units, to SI Units, Multiply by	U.S. Unit	SI Unit	To Convert from SI Units to U.S. Units, Multiply by
25.4	in.	mm	0.03937
0.3048	ft	m	3.281
645.2	in. <sup>2</sup>	mm <sup>2</sup>	1.550 × 10 <sup>-3</sup>
16.39 × 10 <sup>3</sup>	in. <sup>3</sup>	mm <sup>3</sup>	61.02 × 10 <sup>-6</sup>
416.2 × 10 <sup>3</sup>	in. <sup>4</sup>	mm <sup>4</sup>	2.403 × 10 <sup>-6</sup>
0.09290	ft <sup>2</sup>	m <sup>2</sup>	10.76
0.02832	ft <sup>3</sup>	m <sup>3</sup>	35.31
0.4536	lb (mass)	kg	2.205
4.448	lb (force)	N	0.2248
4.448	kip (force)	kN	0.2248
1.356	ft-lb (moment)	N-m	0.7376
1.356	kip-ft (moment)	kN-m	0.7376
16.0185	lb/ft <sup>3</sup> (density)	kg/m <sup>3</sup>	0.06243
14.59	lb/ft (load)	N/m	0.06853
14.59	kip/ft (load)	kN/m	0.06853
6.895	psi (stress)	kPa	0.1450
6.895	ksi (stress)	MPa	0.1450
0.04788	psf (load or pressure)	kPa	20.93
47.88	ksf (load or pressure)	kPa	0.02093
0.566 × (°F - 32)	°F	°C	(1.8 × °C) + 32

**EXAMPLE 2.3-1. Conversion between Systems of Units**

 Convert 23 lb<sub>m</sub> • ft/min<sup>2</sup> to its equivalent in kg • cm/s<sup>2</sup>.

*Solution*

As before, begin by writing the dimensional equation, fill in the units of conversion factors (new/old) and then the numerical values of these factors, and then do the arithmetic. The result is

$$\frac{23 \text{ lb}_m \cdot \text{ft}}{\text{min}^2} \left| \frac{0.454 \text{ kg}}{1 \text{ lb}_m} \right| \left| \frac{100 \text{ cm}}{3.281 \text{ ft}} \right| \left| \frac{1 \text{ min}^2}{(60)^2 \text{ s}^2} \right| \quad (\text{cancellation of units leaves kg} \cdot \text{cm/s}^2)$$

$$= \frac{(23)(0.454)(100) \text{ kg} \cdot \text{cm}}{(3.281)(3600) \text{ s}^2} = \boxed{0.088 \frac{\text{kg} \cdot \text{cm}}{\text{s}^2}}$$

## U.S. Customary System of Units (USCS)

Fundamental Dimension	Base Unit
length [L]	foot (ft)
force [F]	pound (lb)
time [T]	second (s)

Derived Dimension	Unit	Definition
mass [ $F^2/L$ ]	slug	$\text{lb} \cdot \text{s}^2/\text{ft}$

	SI/Metric	Comparable Imperial/US Customary Units
Length	meter (m)	foot (ft) = 0.3048 m yard (yd) = 0.9144 m
	centimeter (cm) = $10^{-2}$ m	inch (in) = 2.54 cm
	kilometer (km) = $10^3$ m	mile (mi) = 1.609 km
Area	square meter ( $\text{m}^2$ )	square foot ( $\text{ft}^2$ ) = 0.0929 $\text{m}^2$ square yard ( $\text{yd}^2$ ) = 0.8361 $\text{m}^2$
	square centimeter ( $\text{cm}^2$ ) = $10^{-4}$ $\text{m}^2$	square inch ( $\text{in}^2$ ) = 6.452 $\text{cm}^2$
	hectare (ha) = $10^4$ $\text{m}^2$	acre (A or ac) = 43,560 $\text{ft}^2$ = 0.4047 ha.
	square kilometer ( $\text{km}^2$ ) = $10^6$ $\text{m}^2$ = 100 ha	square mile ( $\text{mi}^2$ ) = 640 A = 2.590 $\text{km}^2$
Volume	liter (l or L)	gallon (gal) = 3.785 l cubic foot ( $\text{ft}^3$ ) = 7.476 gal = 28.32 l cubic inch ( $\text{in}^3$ ) = 16.39 $\text{cm}^3$
	cubic centimeter ( $\text{cm}^3$ ) = 1 milliliter (ml)	
	cubic meter ( $\text{m}^3$ ) = $10^3$ l	cubic yard ( $\text{yd}^3$ ) = 0.7645 $\text{m}^3$
Temperature <sup>a</sup>	degrees Celsius ( $^{\circ}\text{C}$ )	degrees Fahrenheit ( $^{\circ}\text{F}$ ) = $9/5 (^{\circ}\text{C}) + 32$
Mass <sup>b</sup>	kilogram (kg)	pound (lb) = 0.4536 kg
	gram (g) = $10^{-3}$ kg	ounce (oz) = 1/16 lb = 28.35 g
	metric tonne or metric ton (t) = $10^3$ kg	short ton (commonly called "ton") = 2000 lb = 0.9071 t long ton = 2240 lb = 1.016 t
	quintal (q) = $10^2$ kg	hundredweight (cwt) = 100 lb = 0.4536 q
Force/weight <sup>b</sup>	newton (N)	pound (lb) = 4.448 N
Pressure	pascal (Pa) = 1 $\text{N}/\text{m}^2$	
	kilopascal (kPa) = $10^3$ Pa	pounds per square inch (psi) = 6.893 Pa
	torricelli (torr) = 1 mm of mercury (mm Hg) = 0.1333 kPa 1 bar = $10^5$ kPa	inches of mercury (in Hg) = 25.4 mm Hg = 0.491 psi atmosphere (atm) = 1.013 bar
Energy <sup>c</sup>	joule (J)	foot-pound (ft-lb) = 1.356 J
	calorie (cal) = 4.187 J	
Power	kilocalorie (kcal or Cal) = $10^3$ cal	British thermal unit (Btu) = 1055 J = 0.252 kcal
	watt (W) = joules per second (J/s)	
	kilowatt (kW) = $10^3$ W	horsepower (hp) = 0.7457 kW

## SUMMARY: Units and Conversion

SI is the abbreviation of "Système International d'Unités"

This is the international system of units is based upon :

- seven base units as "length", "time", "temperature", "mass", etc
- two supplementary units
- derived units

### Base units of SI

Base Unit	Name	Name
Length	metre	m
Mass	kilogram	kg
Time	second	s
Electric Current	ampere	A
Temperature	kelvin	K
Luminous Intensity	candela	cd
Amount of Substance	mole	mol

### Supplementary units of SI

Supplementary Units	Name	Name
Plane Angle	radian	rad
Solid Angle	steradian	sr

The derived units may be divided into three groups :

- units which are expressed in terms of base and supplementary units
- units which have been given special names and symbols
- units which are expressed in terms of other derived units

Some **derived units** expressed in terms of base and supplementary units.

Derived Unit	Name	Name
Acceleration	metre / second squared	m / s <sup>2</sup>
Angular Acceleration	radian / second squared	rad / s <sup>2</sup>
Area	square metre	m <sup>2</sup>
Density	kilogram / cubic metre	kg / m <sup>3</sup>
Kinematic Viscosity	square metre / second	m <sup>2</sup> / s
Mass Flow Rate	kilogram / second	kg / s
Molar Mass	kilogram / mole	kg / mol
Specific Volume	cubic metre / kilogram	m <sup>3</sup> / kg
Velocity	metre / second	m / s
Volume	cubic metre	m <sup>3</sup>

Some derived units have special names and symbols.

Derived Units	Name	Symbol
Force	Newton	1 N = 1 kg.m / s
Pressure, Stress	Pascal	1 Pa = 1 N / m
Energy, Work, Quantity of Heat	Joule	1 J = 1 N.m
Power, Radiant Flux	Watt	1 W = 1 J / s
Electric Potential, Potential Difference	Volt	1 V = 1 W / A
Electrical Resistance	Ohm	1 Ω = 1 V / A

Onwards are :

$$\text{kilopascal (kPa)} = 10^3 \text{ N} / \text{m}^2 = \text{kN} / \text{m}^2$$

$$\text{kilonewton (kN)} = 10^3 \text{ kg.m} / \text{s}^2$$

$$\text{kilojoule (kJ)} = 10^3 \text{ N.m} = \text{kN.m}$$

### Conversion Table

From the old (metre-kilogram-second-ampere) system to units of SI.

1 Bar	= 100 kPa (0.1 N / mm <sup>2</sup> )
1 Btu (British Thermal Unit)	= 1.055 kJ = 1055 J
1 cP (Centipoise)	= 10 <sup>-3</sup> Pa.s
1 cSt. (Centistokes)	= 10 <sup>-6</sup> m <sup>2</sup> / s
1 dyne	= 1 g.cm / s <sup>2</sup> = 10 N
1 erg	= 1 dyn.cm = 10 J
1 hp (Horsepower)	≈ 745.7 W
1 kcal	= 4.1868 kJ = 4186.8 J
1 kcal / h	= 1.163 W
Kelvin	≈ °C + 273
1 mbar (Milibar)	= 100 Pa
1 mmHg (Torr)	≈ 133.32 Pa
1 mwc	≈ 9.81 kPa (9.81 kN / m <sup>2</sup> )
1 pk (paardekracht NL)	≈ 735.5 W
1 psi	≈ 6.89 kPa (6.89 kN.m <sup>2</sup> )
1 kgf	≈ 9.81 N
1 kgf / cm <sup>2</sup>	≈ 98.07 kPa

1 in	= 1 inch	= 25.4 x 10 <sup>-3</sup> m
1 ft	= 1 foot	= 0.3048 m
1 in <sup>2</sup>	= 1 inch <sup>2</sup>	= 0.64516 x 10 <sup>-3</sup> m <sup>2</sup>
1 ft <sup>2</sup>	= 1 foot <sup>2</sup>	= 0.0929 m <sup>2</sup>
	1 lb	= 0.454 kg
	1 lb / h	≈ 0.12599 x 10 <sup>-3</sup> kg / s
	1 in <sup>3</sup>	≈ 16.387 x 10 <sup>-6</sup> m <sup>3</sup> (= 16.387 cm <sup>3</sup> )
	1 UK gal	≈ 4.546 x 10 <sup>-3</sup> m <sup>3</sup> (= 4.546 dm <sup>3</sup> )
	1 US gal	≈ 3.785 x 10 <sup>-3</sup> m <sup>3</sup> (= 3.785 dm <sup>3</sup> )

# Dimensional Consistency: Examples

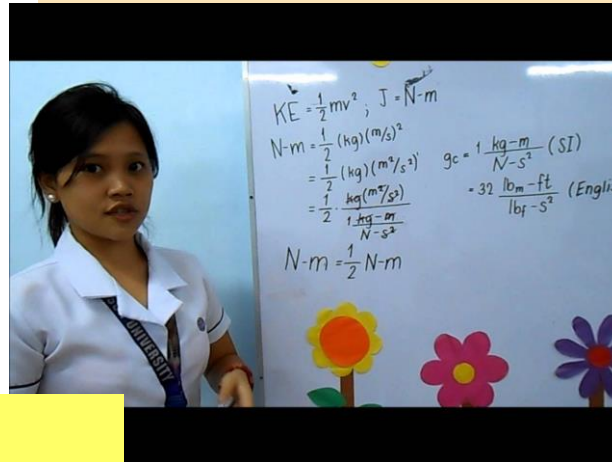
## DIMENSIONAL ANALYSIS

### Dimensional consistency

distance velocity time distance

$$x = vt + x_0$$

$$[L] = \frac{[L]}{[T]} [T] + [L] = [L] + [L] = [L]$$



## Two Examples of Equations with Dimensional Consistency

$$x = vt$$

Using dimensions

$$[L] = \frac{[L]}{[T]} [T]$$

Using units

$$m = \left(\frac{m}{s}\right) s = m$$

$$v^2 = v_0^2 + 2a(x - x_0)$$

Using dimensions

$$\left(\frac{[L]}{[T]}\right)^2 = \left(\frac{[L]}{[T]}\right)^2 + \frac{[L]}{[T]^2} ([L] - [L])$$

$$\left(\frac{[L]}{[T]}\right)^2 = \left(\frac{[L]}{[T]}\right)^2 + \frac{[L]}{[T]^2} ([L])$$

Using units

$$\left(\frac{m}{s}\right)^2 = \left(\frac{m}{s}\right)^2 + \frac{m}{s^2} (m - m)$$

$$\left(\frac{m}{s}\right)^2 = \left(\frac{m}{s}\right)^2 + \frac{m}{s^2} (m)$$

### Dimensional consistency

- A basic principle states that equations must be **dimensionally consistent**.
- Using *van der Waal's* equation as an example,

#### Example 4

What are the dimensions of *a* and *b*?

$$\left(p + \frac{a}{V^2}\right)(V - b) = RT$$

- 'a' has the units (pressure)(volume)<sup>2</sup>
- 'b' has the same units as 'V' [volume]

#### Dimensionless numbers

- There are some variables or group of variables that do not have a net unit. These are called **non-dimensional** or **dimensionless** variables, for example,

$$N_{RE} = \frac{Dv\rho}{\mu} \quad \begin{array}{c|c|c|c} \text{cm} & \text{cm} & \text{g} & (\text{cm})(\text{s}) \\ \hline & \text{s} & \text{cm}^3 & \text{g} \end{array}$$

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SKMM1922: Technical Problem Solving

## **ESTIMATION IN ENGINEERING**

In the earlier stages of design, engineers nearly always make approximations when solving technical problems. Those estimates are made to reduce a real system, as imperfect and non-ideal as it may be, into its most basic and essential elements.

- Assumption (inviscid, adiabatic, isothermal and etc)
- Linearised
- Simplified model
- Boundary Conditions
- Uncertainties
- Time and Cost



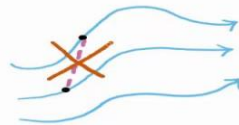
## Examples of engineering estimation:

### 1. Bernoulli's Equation [assumptions: steady, inviscid and incompressible flow]

$$\frac{1}{2} \rho v^2 + \rho g h + p = \text{constant (along a streamline)}$$

Assumptions

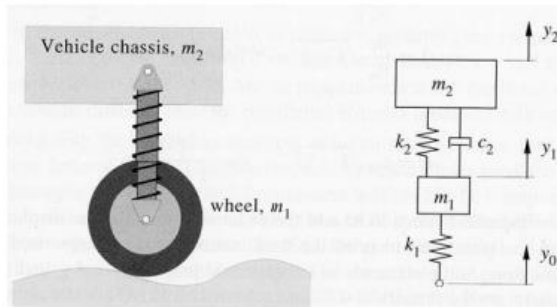
Applied along a streamline →



$$\frac{V_1^2}{2g} + \frac{p_1}{\rho g} + z_1 = \frac{V_2^2}{2g} + \frac{p_2}{\rho g} + z_2$$

### 2. Mass-spring-damper to model vehicle suspension

A car and its suspension system traveling over a bumpy road can be modeled as a mass/spring/damper system. In this model,  $y_1$  is the vertical motion of the wheel center of mass,  $y_2$  is the vertical motion of the car chassis, and  $y_0$  represents the displacement of the bottom of the tire due to the variation in the road surface.

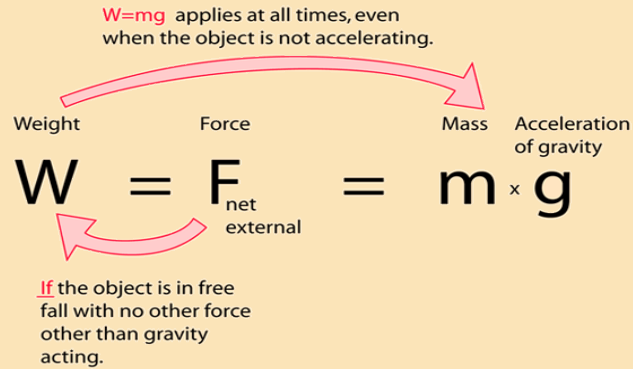


Spring/mass/damper model for an automobile suspension system.



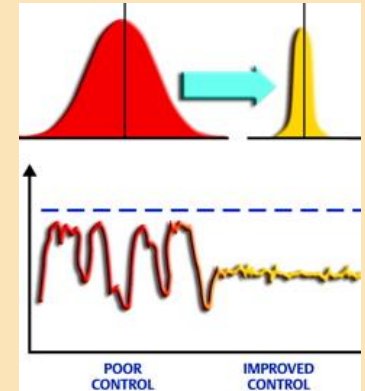
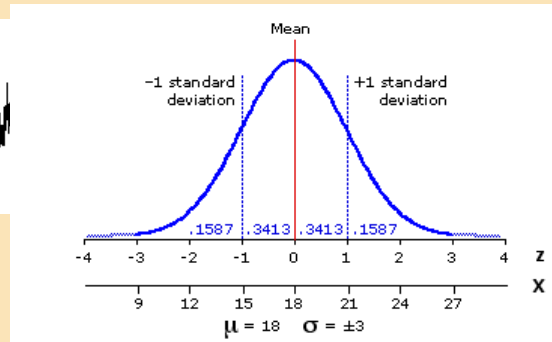
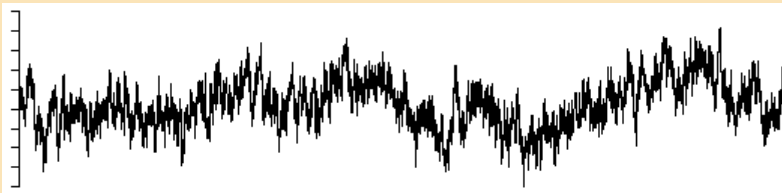
### (3) Variation in gravity

*g values (m/s<sup>2</sup>):*  
 Standard = 9.80665  
 Equatorial = 9.78033



### (4) Fluctuation in data and signal measurement (Systematic Error + Random Error)

*Statistics: Mean, Root-Mean-Square (RMS) and Standard Deviation (Sigma)*



# Resources

# RESOURCES

1. Dr. Mohd. Shuisma bin Mohd. Ismail (2011), Chairman FYE Committee, Faculty of Mechanical Engineering, UTM - ***Notes and Personal Communication***
2. Dr. Eric P. Soulsby, ***University Learning Skills: A First Year Experience Orientation Course for Engineers***, 29th ASEE/IEEE Frontiers in Education Conference Session 11a7-6
3. Donald F. Elger, Terry R. Armstrong, Steven W. Beyerlein, Carlo F. Felicione, Katharine J. Fulcher, Paul W. Rousseau (2001), ***A Structured Problem Solving Model for Developing High-Level Skills***, Proceedings of the American Society for Engineering Education Annual Conference & Exposition
4. N. J. Mourtos, N. DeJong Okamoto & J. Rhee (2004), ***Defining, teaching, and assessing problem solving skills***, 7th UICEE Annual Conference on Engineering Education UICEE, Mumbai, India
5. Wales, C.E., and Stager, R.A., (1990), ***Thinking With Equations***, Center for Guided Design, West Virginia University, Morgantown, WV.
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